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Tree-Adjoining Grammars: Theory and implementation

Day 3 – part I

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Tree templates and tree families

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- is a set of *tree templates*
- represents a subcategorization frame, and
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- transitive: `Tnx0Vnx1`

  tree templates: base tree, passive with *by*, wh-moved subject, wh-moved object, imperative, determiner gerund, ... etc.

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  - topicalization
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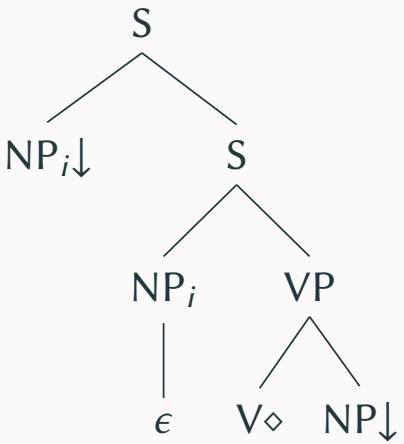
- filler-gap constructions, e.g.
  - topicalization
  - wh-movement
- long-distance dependencies $\Rightarrow$ **extraction**
  - subject extraction (α`W0nx0V`)
  - object extraction (α`W1nx0Vnx1`)
  - preposition stranding (α`W1nx0VPnx1`)
  - AP complement extraction (α`W1nx0Vnx1`)

Extraction: tree templates

subject extraction

(α`W0nx0Vnx1`)



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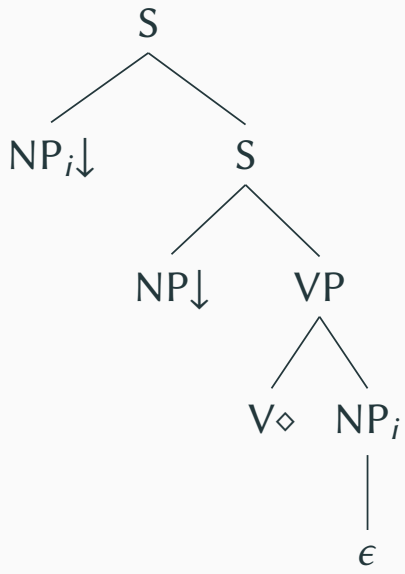

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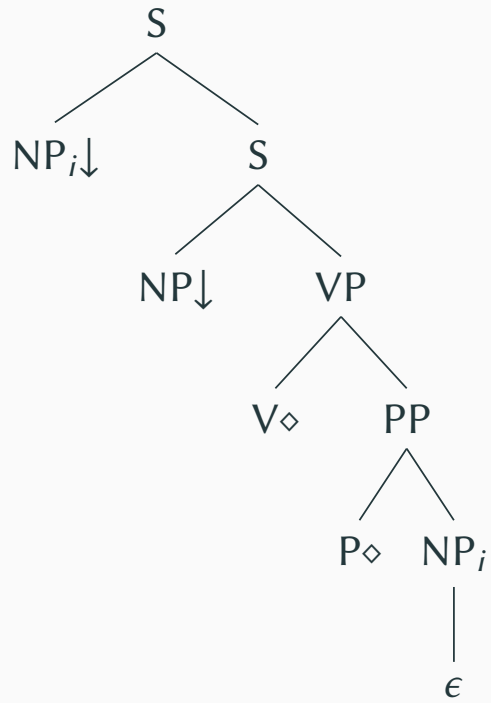

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	c.	Mia$_i$, Pim gave a book to _$_i$.	(NP from PP)
	d.	To Mia$_i$, Pim gave a book _$_i$.	(PP)
	e.	*Pim, _$_i$ gave a book to Mia.	(no subject topicalization!)

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- unbounded dependency → the dependency between an extracted constituent and its trace may extend across more *clause boundaries*

(2)
a. The book$_i$, Bill knows (that) Joe loves _$_i$.
b. The book$_i$, Tom believes (that) Bill knows (that) Joe loves _$_i$.

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  *Whom$_i$ does Sam know the student that likes _$_i$?

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- *wh*-questions involve **subject-auxiliary inversion**: the auxiliary verb (*do*, *have*, *be*, …) precedes the subject

Subject-auxiliary inversion

- **Obligatory subject-auxiliary inversion** in direct questions with object extraction:

(1) a. What$_i$ **does** John read _$_i$?
b. *What$_i$ John **does** read _$_i$?
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- **No subject-auxiliary inversion** in embedded wh-questions:

(2) a. I wonder [what$_i$ John reads _$_i$].
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Subject-auxiliary inversion

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  (2) a. I wonder [what$_i$ John reads _$_i$].
  b. *I wonder [what$_i$ **does** John read _$_i$].

- **No subject-auxiliary inversion** in topicalization:

  (3) a. *[The meeting]$_i$, **have** John missed _$_i$.
  b. [This meeting]$_i$ John **have** missed _$_i$.

Extraction: features

Features for extraction:

- <**extracted**> := + | − indicate extraction in the S-node
- <**wh**> := + | − indicate the presence of a wh-pronoun
- <**inv**> := + | − indicate inversion

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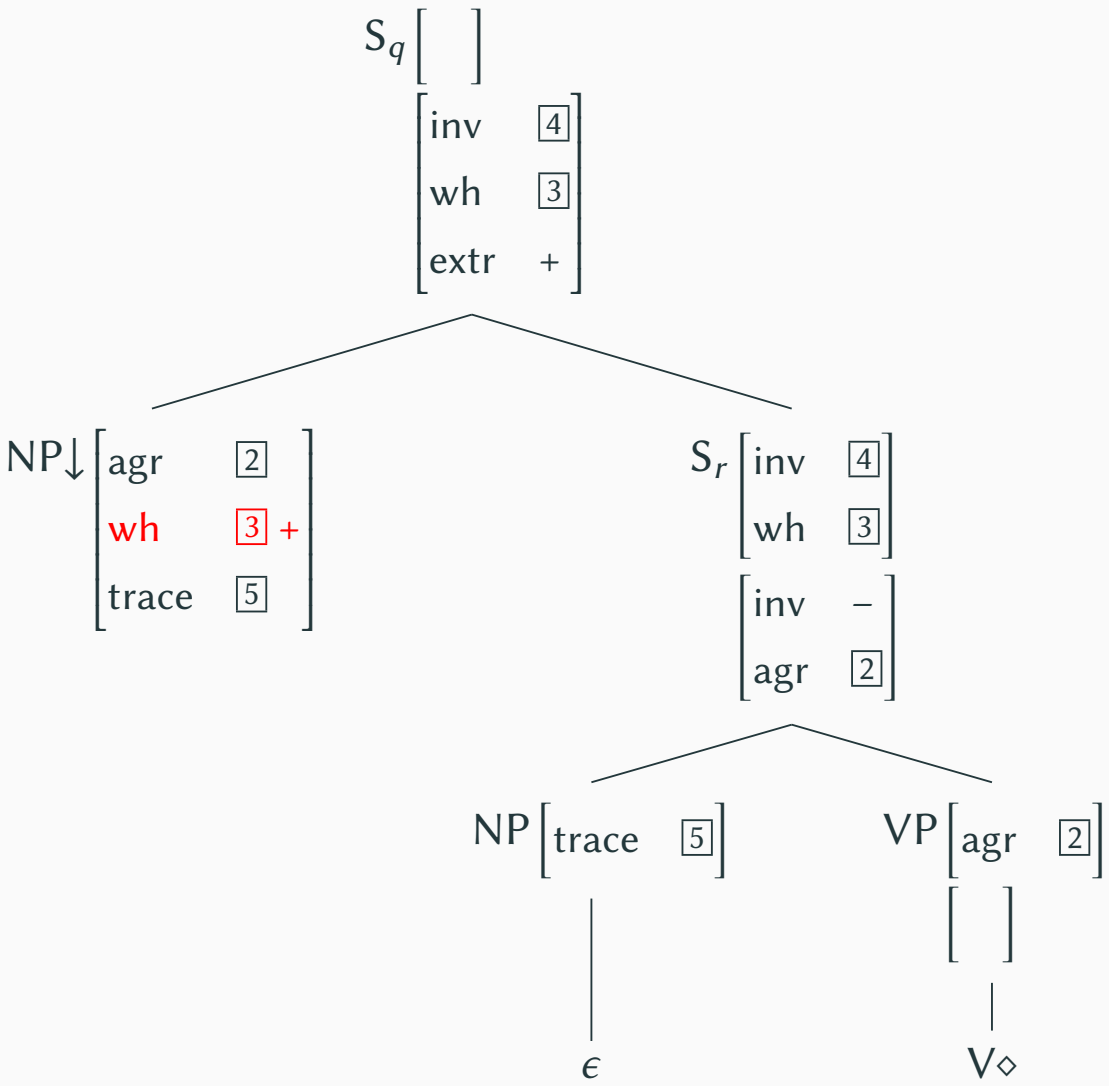
Capturing:

- no inversion with topicalization (*Books$_i$, people read _$_i$.*)
- no topicalized subject (**People$_i$, _$_i$ read books.*)
- no inversion with subject wh-extraction (*Who$_i$ _$_i$ read books?*)
- inversion with object wh-extraction (*What$_i$ do people read _$_i$?*)

Extraction: tree templates with features

Tree template for subject extraction (simplified); αW0nx0V



$\Rightarrow$ subject extraction only for *wh*-phrases; no topicalized subject

Inversion with object extraction

- in case of object extraction
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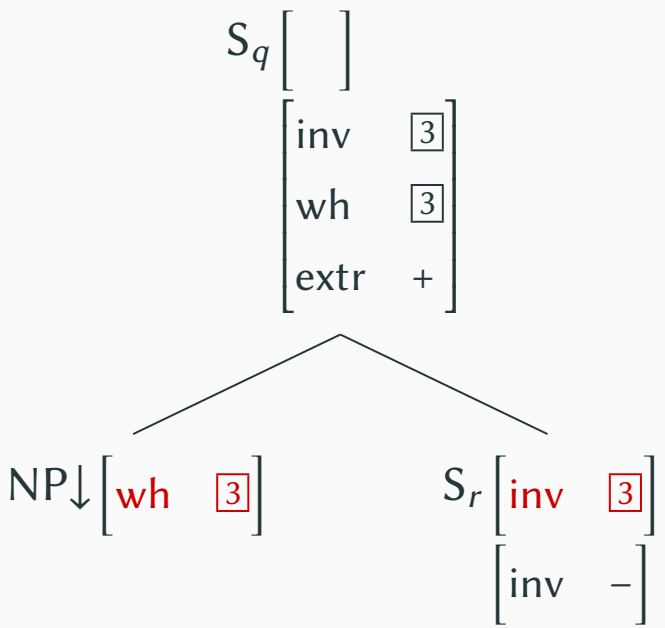
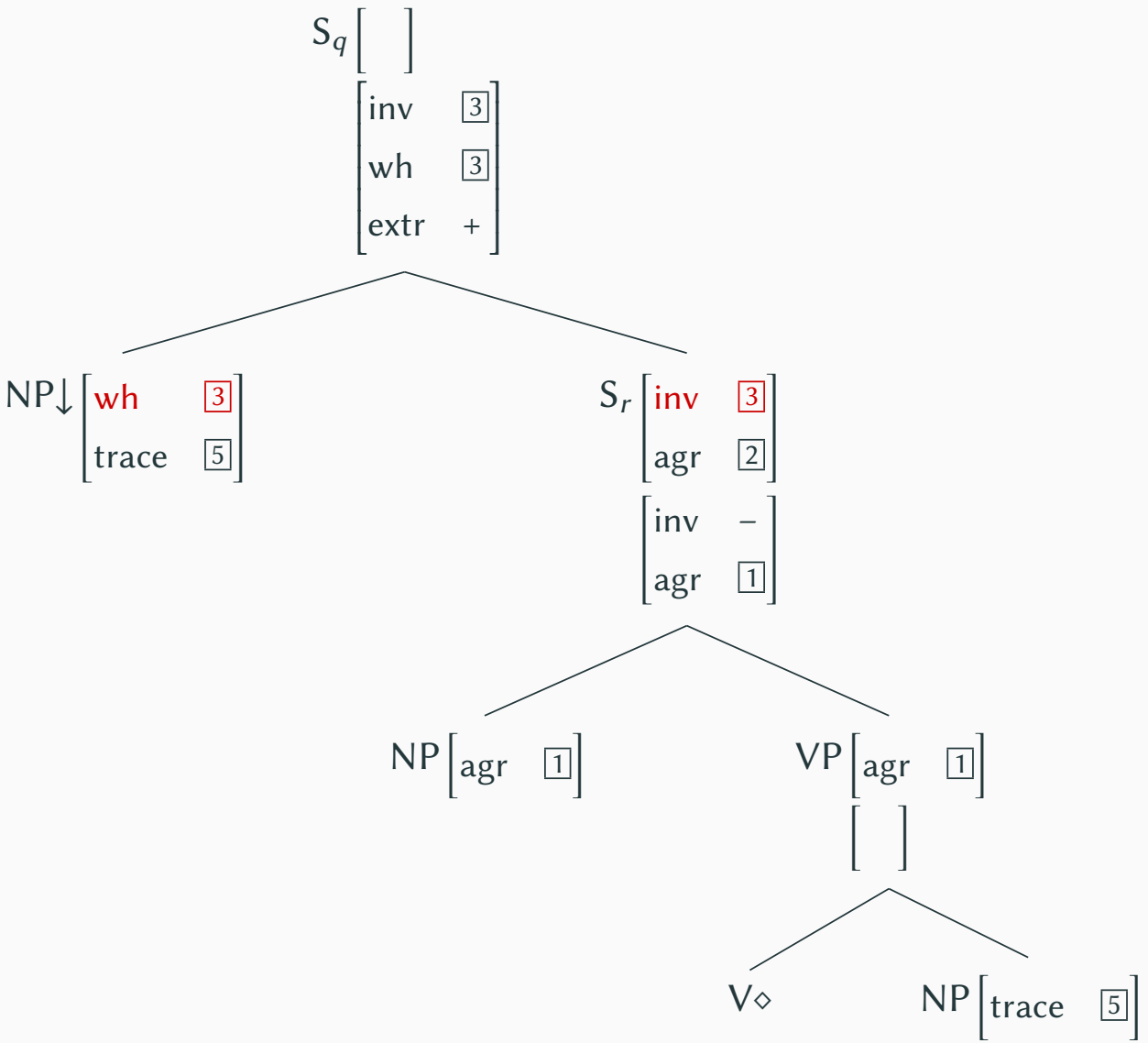
  S_r: top.<**inv**> and the extracted NP: top.<**wh**>



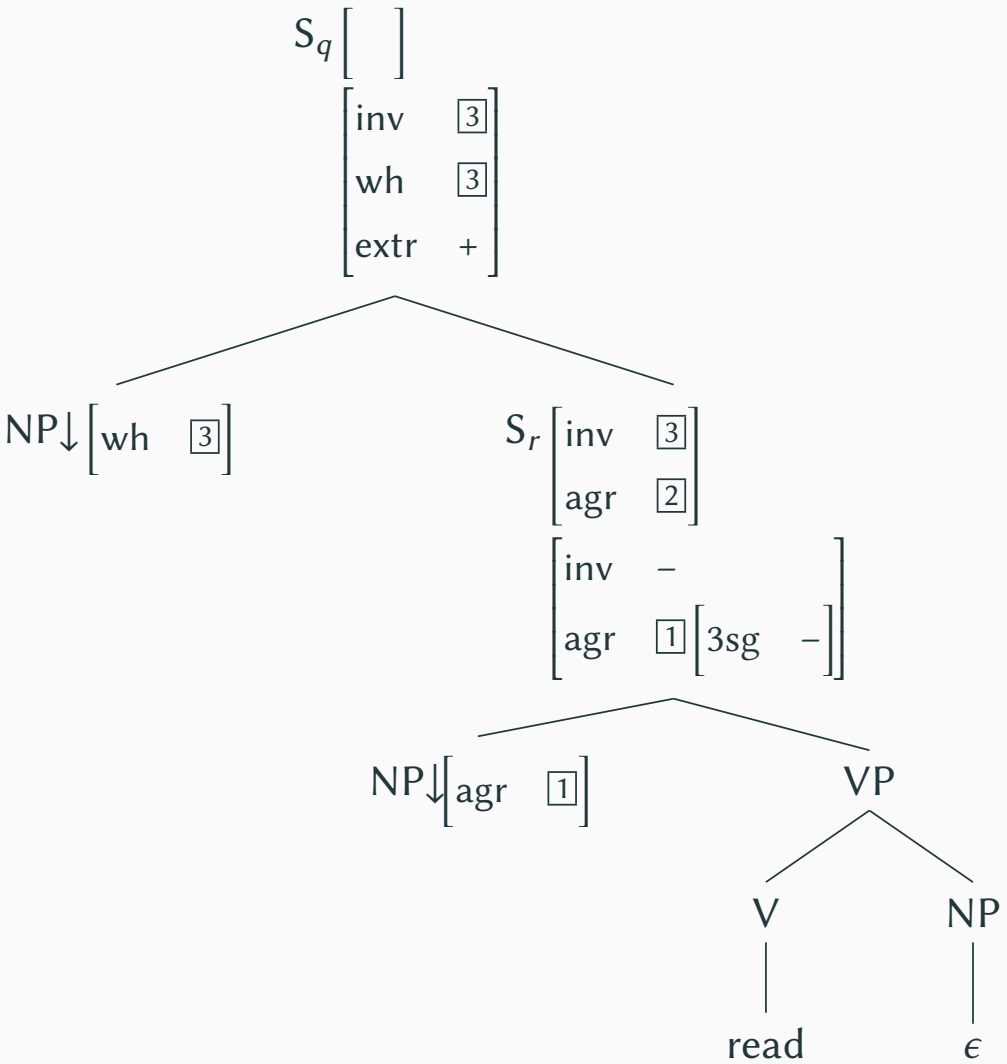
Extraction: tree templates with features

Tree template for object extraction (simplified!); αW1nx0Vnx1

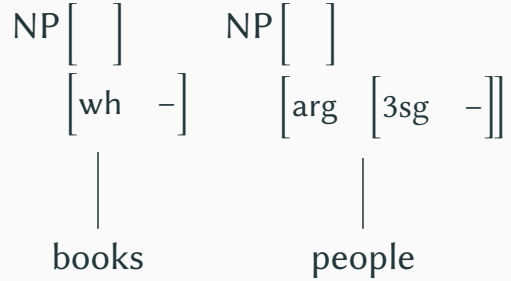


Analyses

Books, people read.



NP-trees to substitute (subj, obj):



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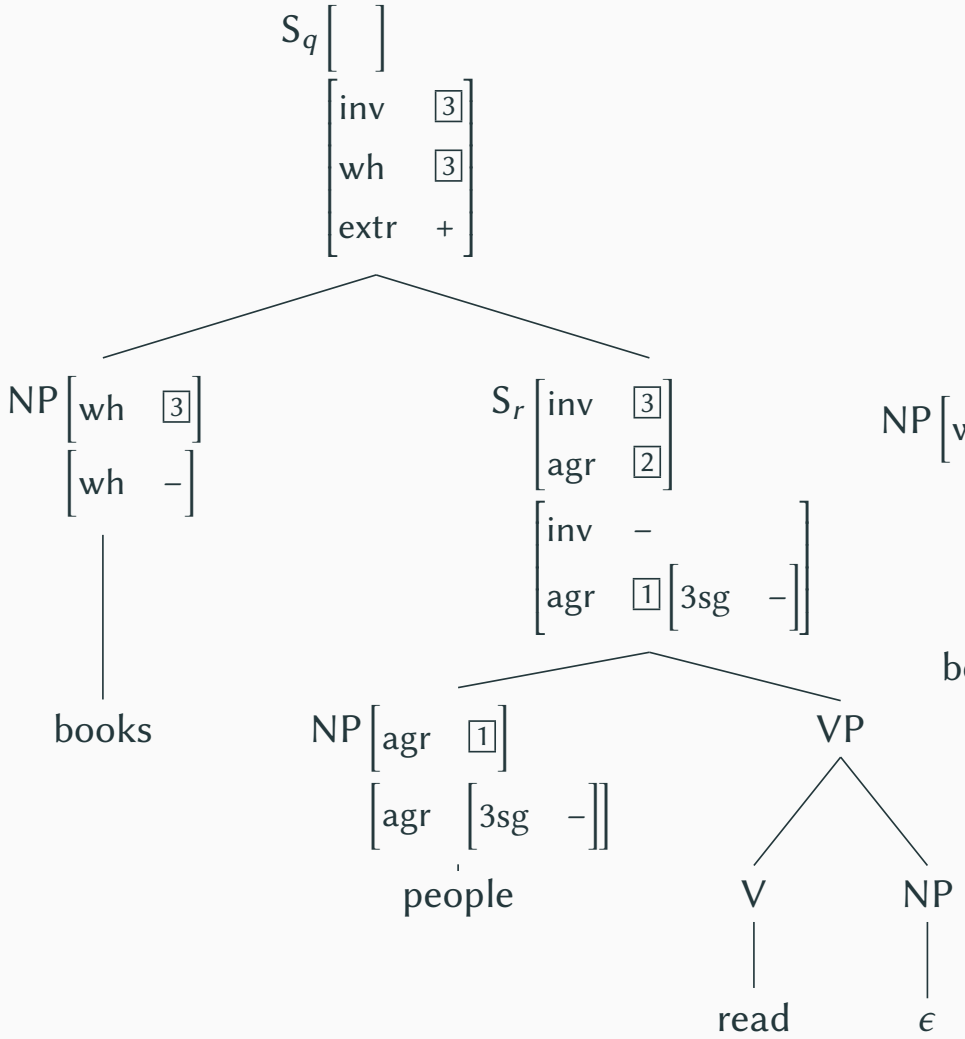

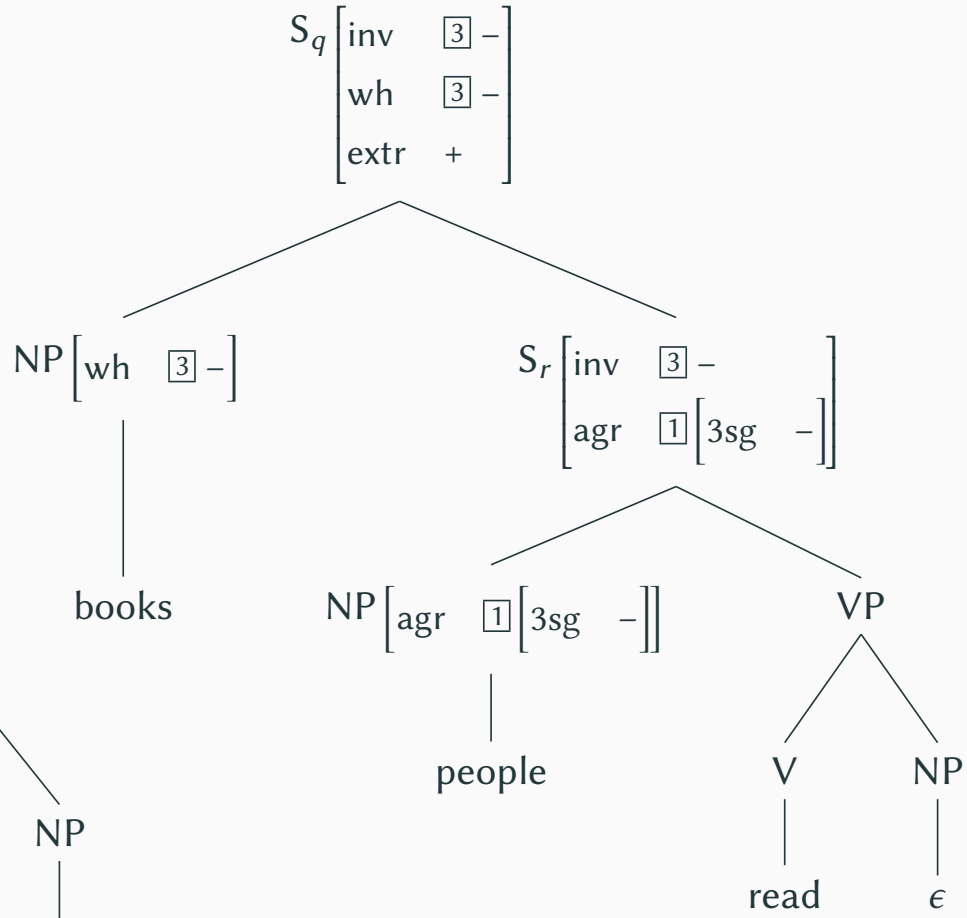

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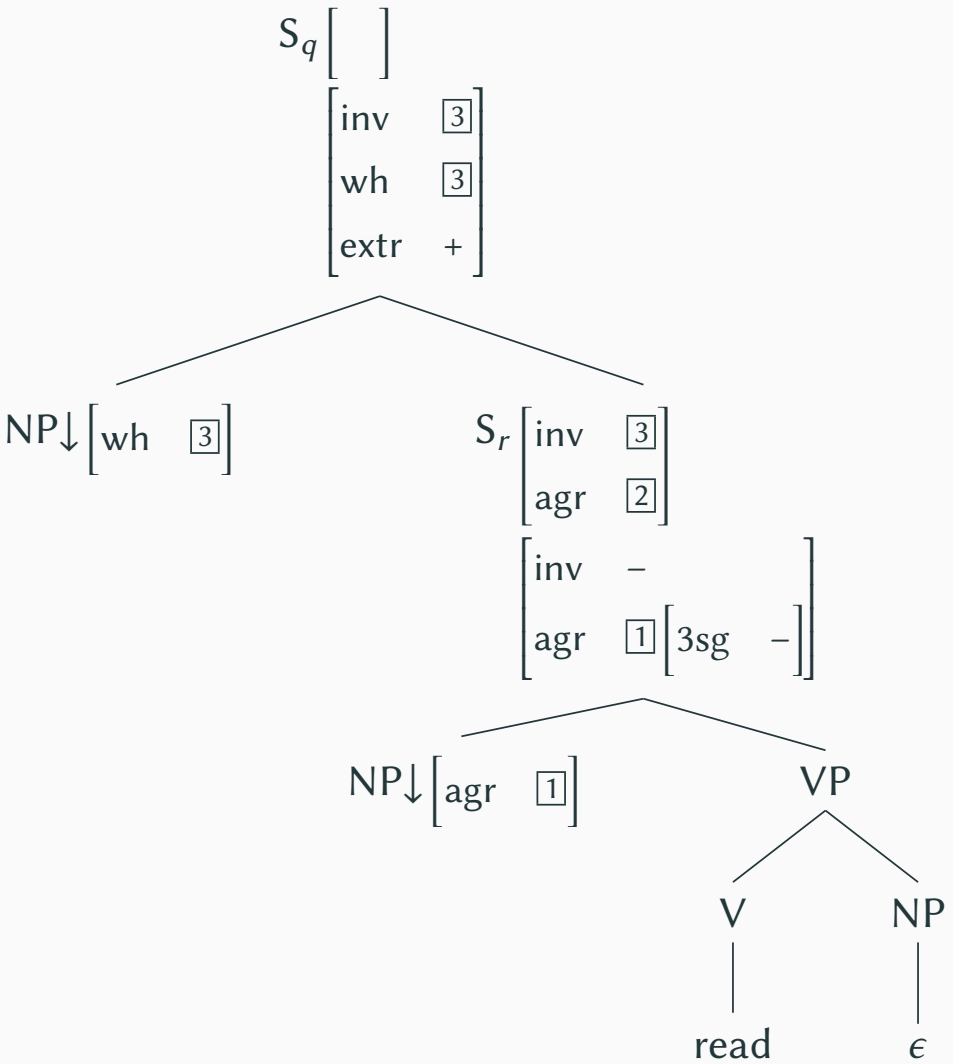
What do people read?



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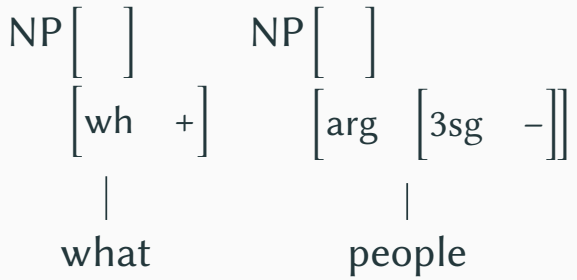

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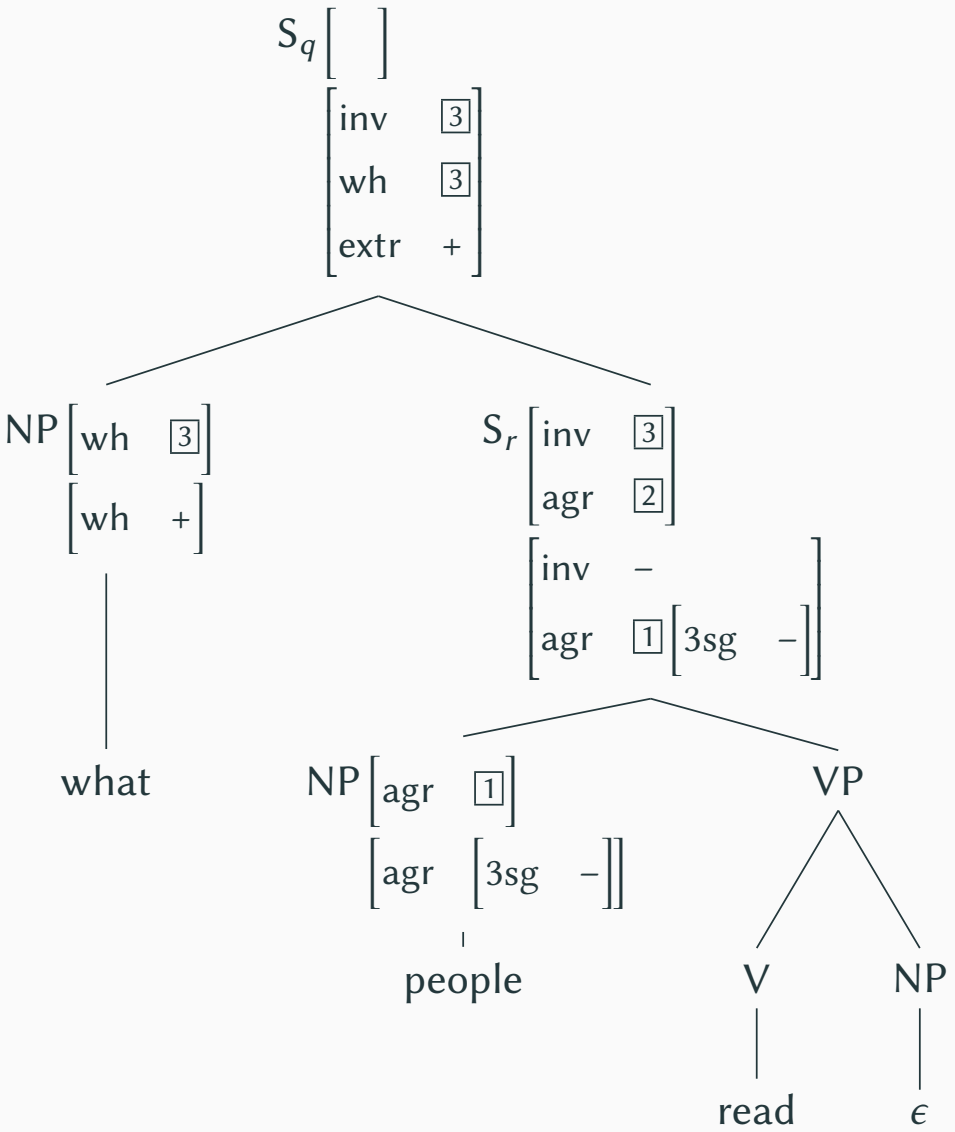
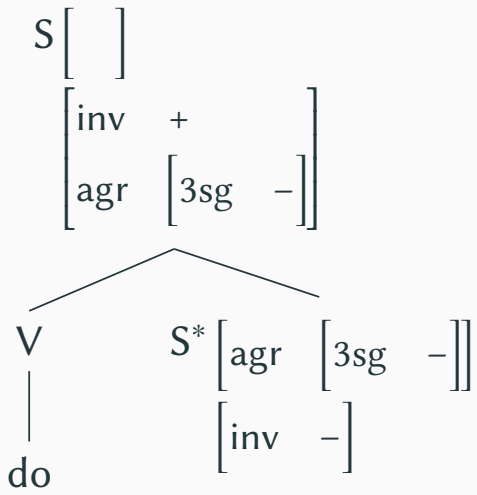


- cannot end the derivation here
- forcing adjunction at S_r
- adjoin the tree of 'do'



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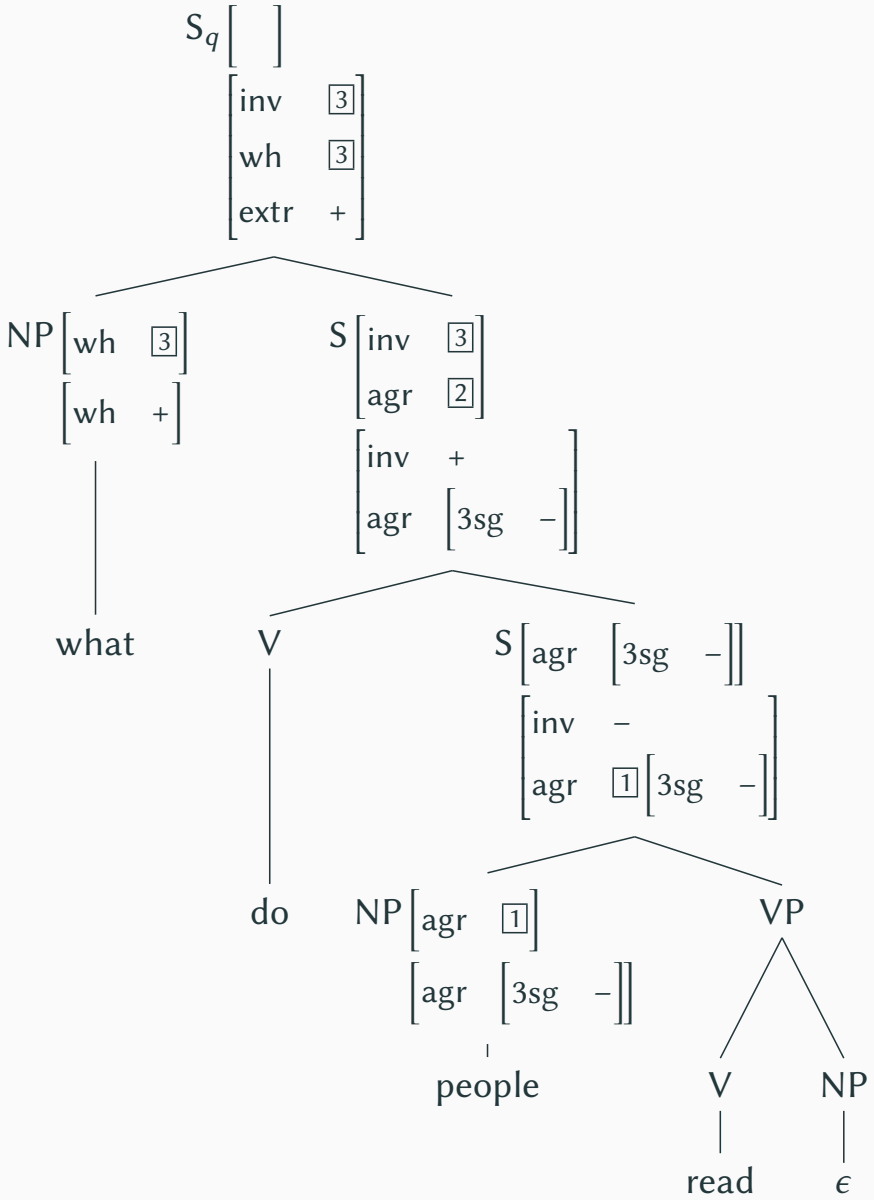

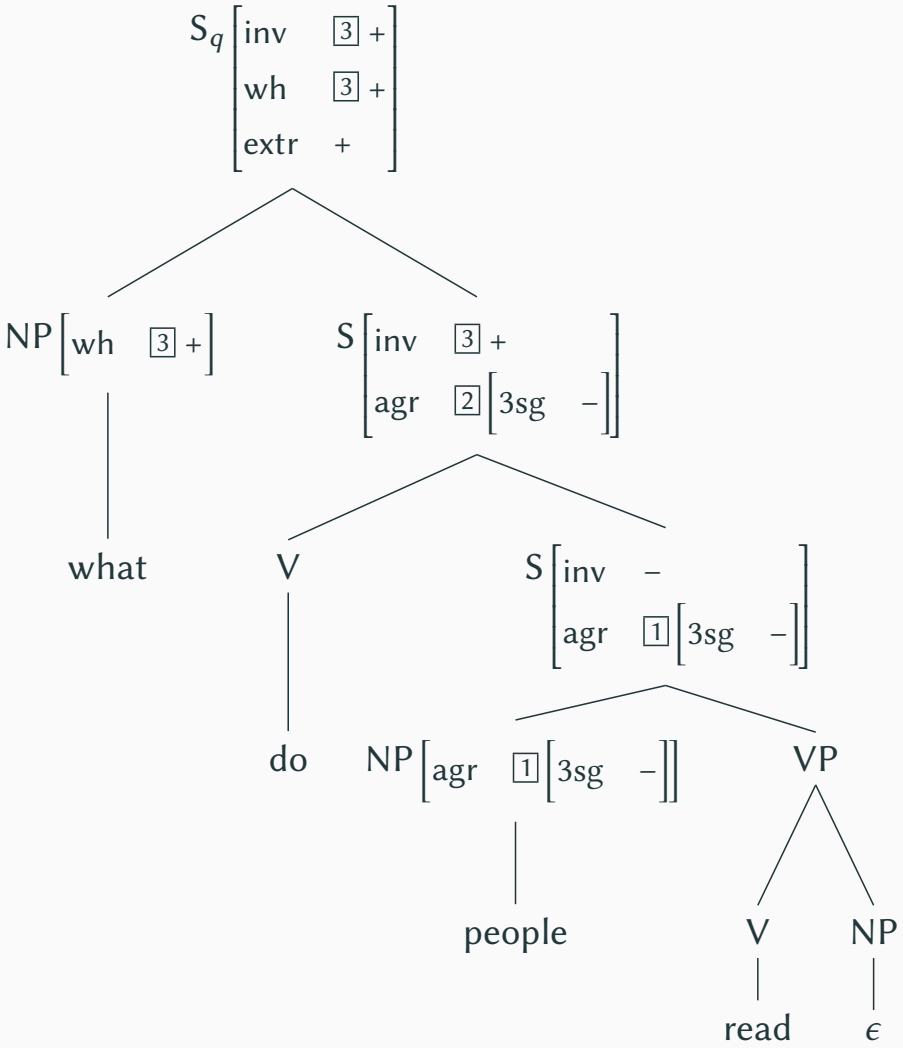

LTAG semantics: overview

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Three principal approaches:

1. LTAG semantics with synchronous TAG (STAG)

   [Shieber 1994, Nesson & Shieber 2006, 2008]

2. unification based LTAG semantics with predicate logic

   [Kallmeyer & Joshi 2003, Gardent & Kallmeyer 2003, Kallmeyer & Romero 2008]

3. unification based LTAG semantics with frames

   [Kallmeyer & Osswald 2013, Kallmeyer & Osswald & Pogodalla 2016]

Synchronous TAG (STAG)

Idea:

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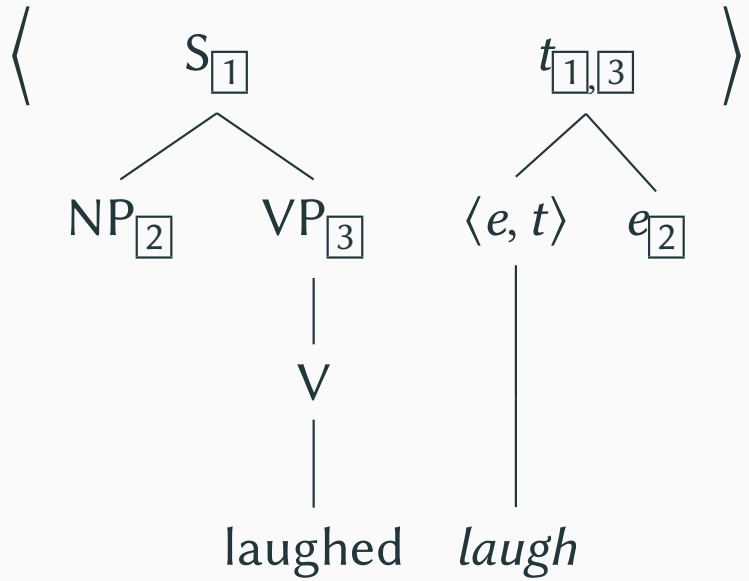
More precisely, it contains pairs $\langle \gamma_1, \gamma_2, \mathit{link} \rangle$ where γ_1 is an elementary tree from G_1, γ_2 an elementary tree from G_2, and *link* is a set of pairs of node addresses from γ_1 and γ_2 respectively.

LTAG semantics: STAG



(The links are shown with boxed numbers.)

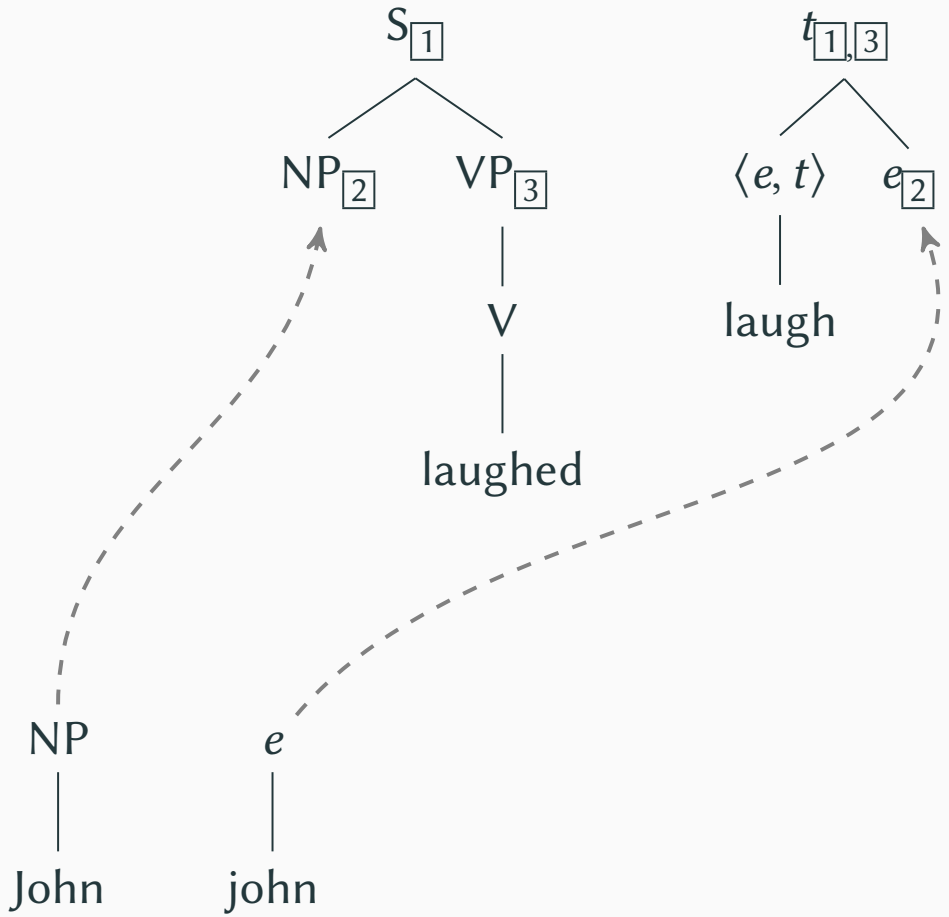
- The non-terminals of the semantic TAG are types t, e, $\langle e, t\rangle$, ...
- The semantic TAG describes the syntactic structure of typed predicate logical formulas.
- The links in this example tell us, for instance, that the subject NP corresponds to the e argument of *laugh*.

LTAG semantics: STAG

STAG derivation proceeds as in TAG, except that all operations must be paired. In every derivation step:

- A new elementary tree pair $\langle \gamma_1, \gamma_2 \rangle$ is picked.
- γ_1 is attached (substituted or adjoined) to the syntactic tree while γ_2 is attached to the semantic tree.
- The nodes that the two trees attach to must be linked.
- The link that is used in this derivation step disappears while all other links involving the attachment sites are inherited by the root of the attaching tree.

LTAG semantics: STAG



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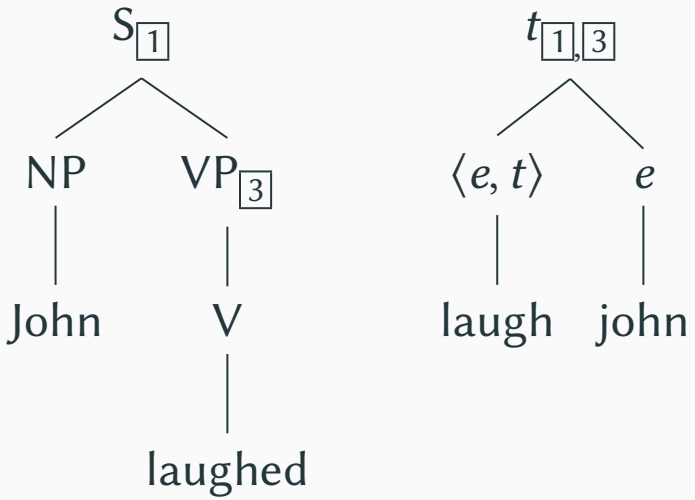

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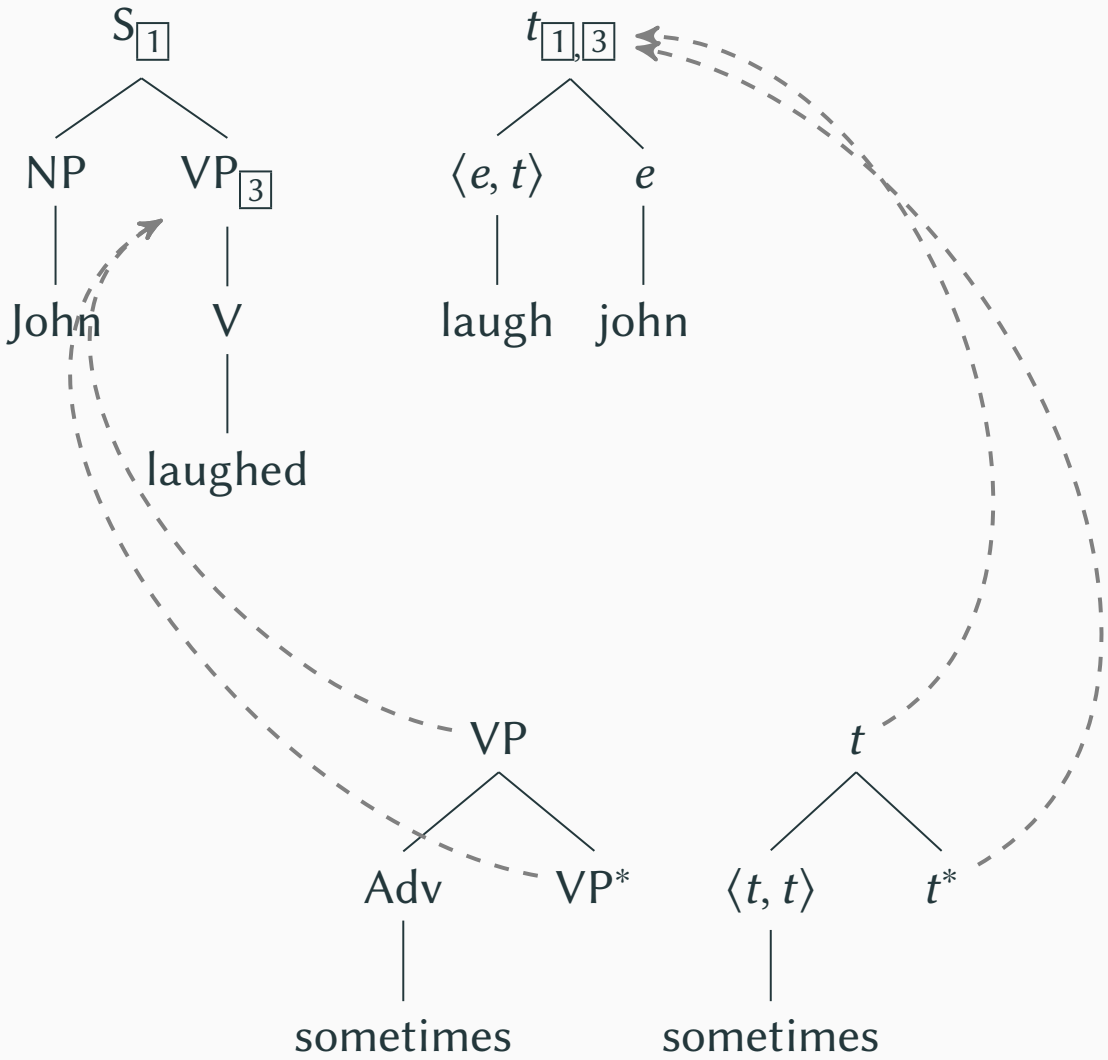

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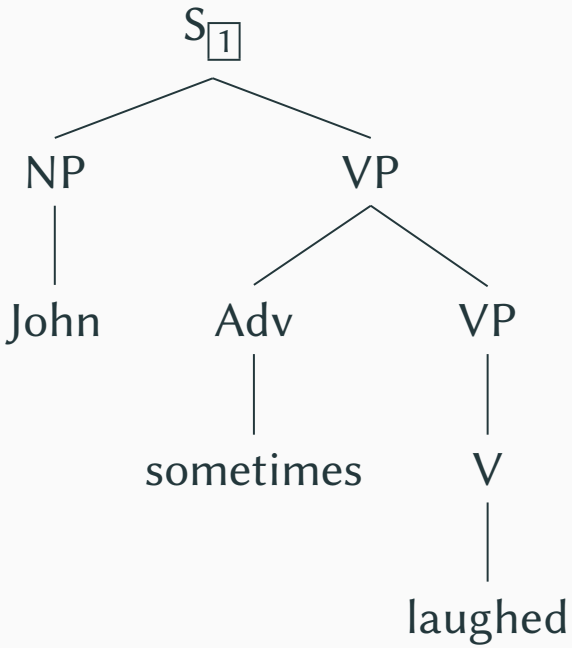

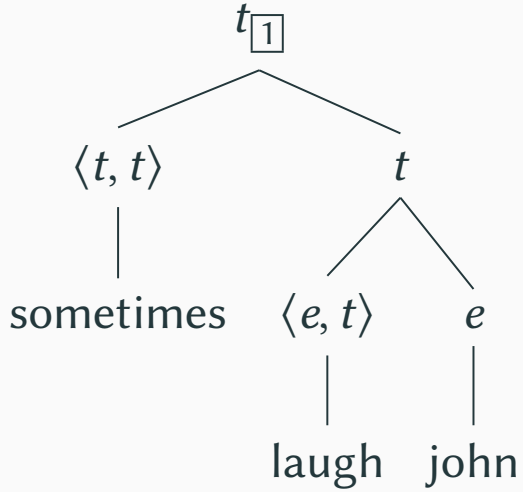

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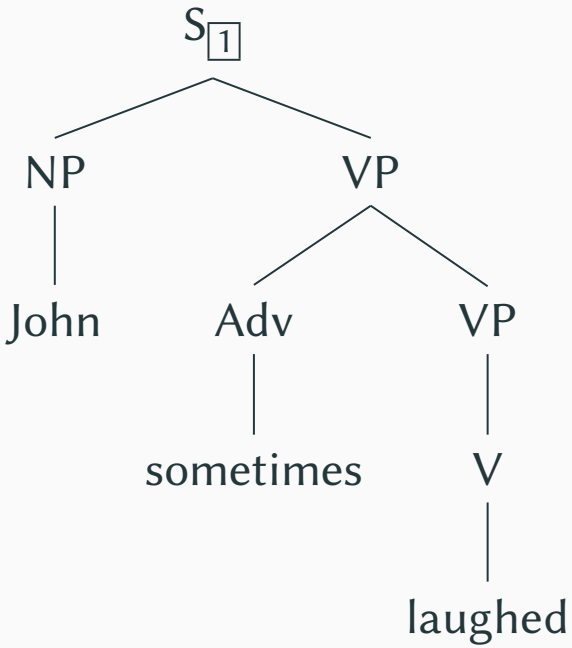
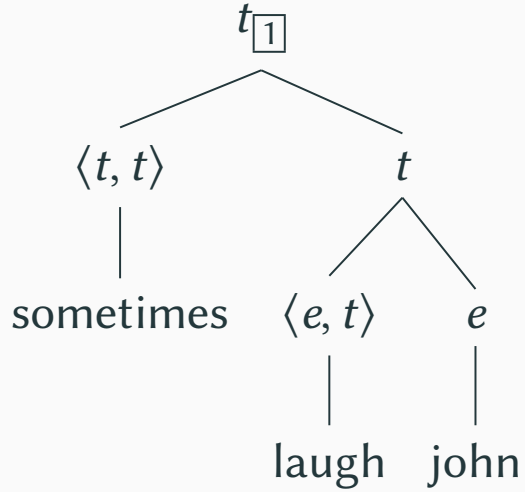




Logical form: sometimes(laugh(john))

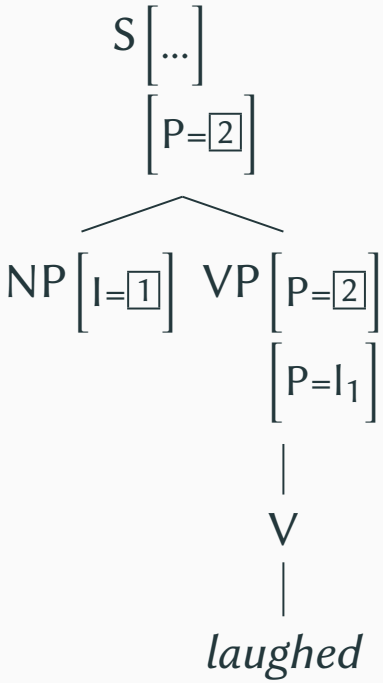
Unification-based LTAG semantics with predicate logic

- syntax-semantics interface for LTAG
- Idea: each elementary tree is paired with
  - a set of **typed predicate logic expressions** and
  - a set of **scope constraints** (i.e., constraints on sub-term relations)
  - **interface features** that characterizes
    a) which arguments need to be filled,
    b) which elements are available as arguments for other elementary trees and
    c) the scope behaviour.

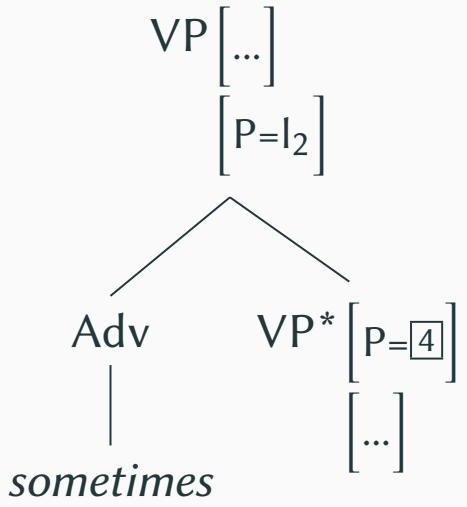
  The features are linked to positions in the elementary tree.

Unification-based LTAG semantics with predicate logic

$l_3 : pim(x)$

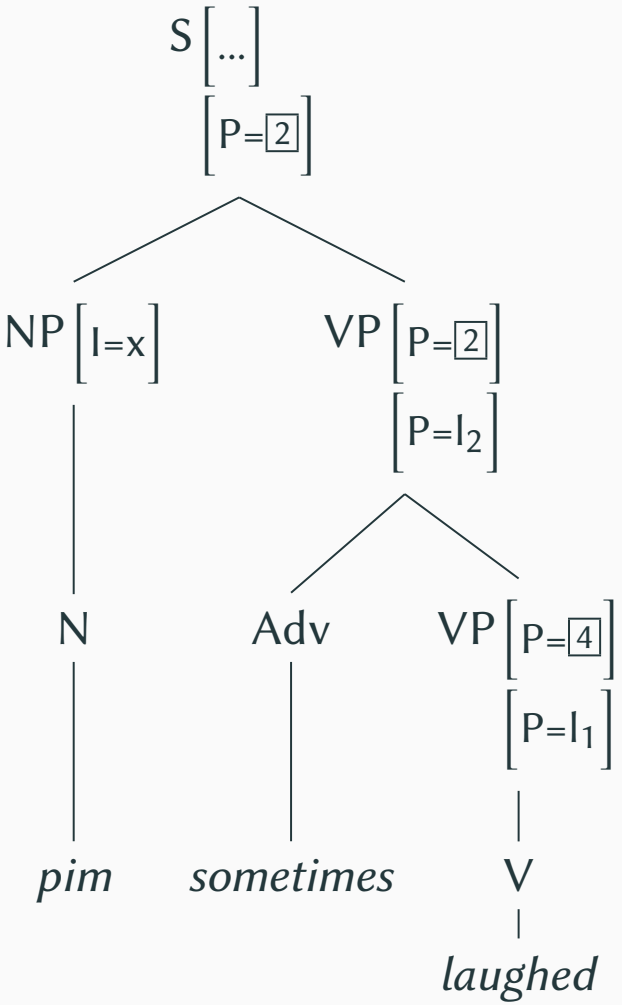


$l_1 : laugh(1)$



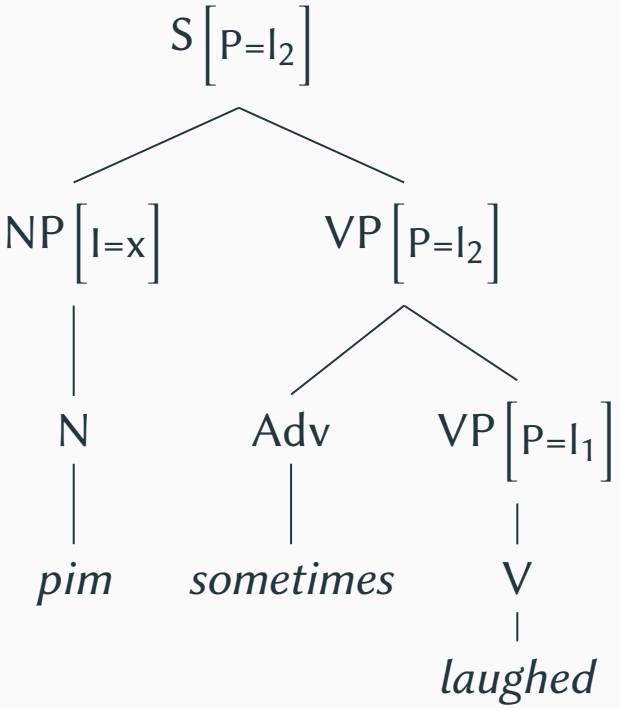
$l_2 : sometimes(3), 3 \lhd^* 4$

Unification-based LTAG semantics with predicate logic



$l_1 : laugh(x)$,
$l_3 : pim(x)$,
$l_2 : sometimes(\boxed{3})$,
$\boxed{3} \lhd^* \boxed{4}$

Unification-based LTAG semantics with predicate logic



$l_1 : laugh(x)$,
$l_3 : pim(x)$,
$l_2 : sometimes(\boxed{3})$,
$\boxed{3} \lhd^* l_1$

- $\boxed{3} \lhd^* l_1$ signifies that the formula labeled l_1 is a subformula of the formula that has to be placed in the hole $\boxed{3}$
- disambiguation leads to $pim(x) \wedge sometimes(laugh(x))$

Unification-based LTAG semantics with frames

- Semantic representations are linked to entire elementary trees (as in the previous approaches).
- Semantic representations: frames, expressed as typed feature structures.
- Interface features relate nodes in the syntactic tree to nodes in the frame graph.
- Frame composition by unification, triggered by the unifications on the interface features that are in turn triggered by substitution, adjunction and final top-bottom unification on the derived tree.

Unification-based LTAG semantics with frames

(4) Pim ate an apple.